

Midterm

Name: _____

Student No. _____

- Time: 90 Minutes, Total Marks: 25
- Interaction with another student is NOT allowed

- Closed book exam. NO additional materials are allowed
- Calculators are NOT allowed

Q1. Write down the 6-bits binary representation for each of the following numbers: (1.5+1.5=3 mark)

(a) $(+16)_{10}$
Sign magnitude: 0 10000

1's complement: 010000

2's complement: 110000

010000
+ 1111
101111
+ 1
110000

(b) $(-16)_{10}$
Sign magnitude: 1 10000

1's complement: 110000

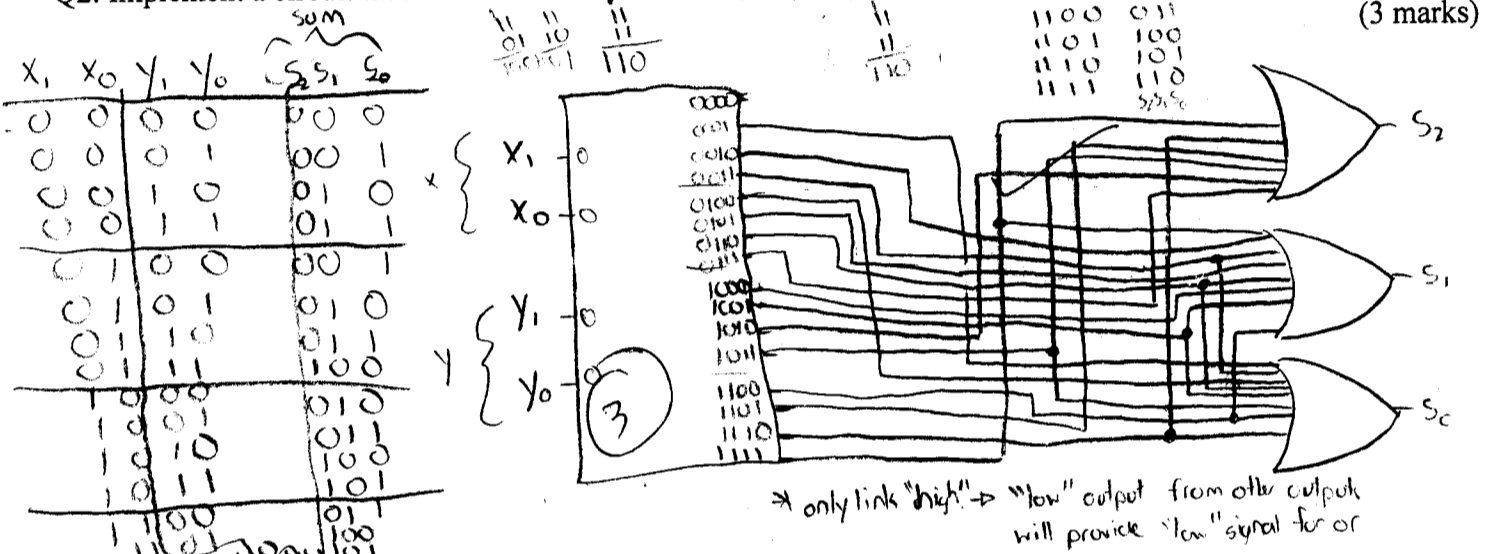
2's complement: 010000

$\frac{16}{2} = 8 \neq 0$
 $\frac{8}{2} = 4 \neq 0$
 $\frac{4}{2} = 2 \neq 0$
 $\frac{2}{2} = 1 \neq 0$
 $\frac{1}{2} = 0 = 1$

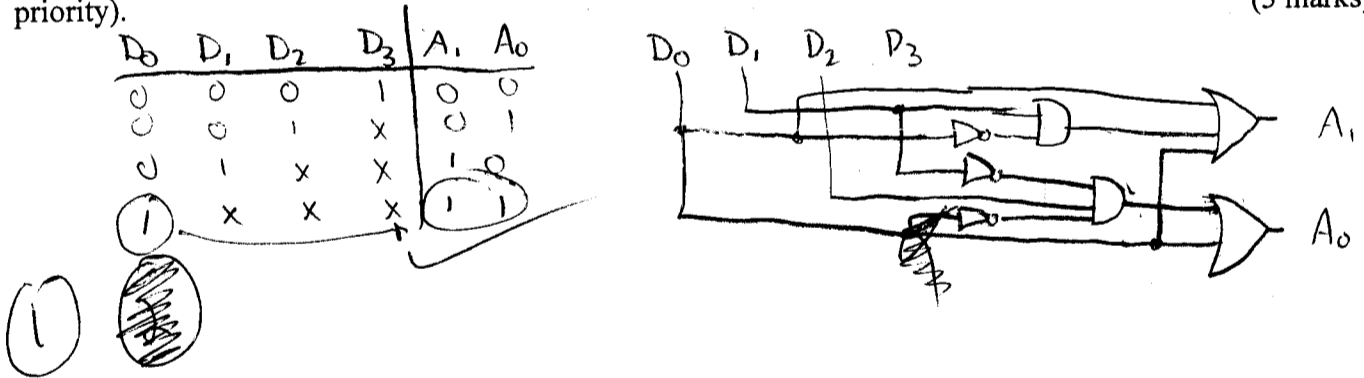
Q2. What is a Tristate gate? Explain its operation. (1 mark)

A tristate gate allows the input to pass to the output if it is enabled. If it is not enabled, the output is High-Z.

Q2. Implement a circuit that adds two binary numbers, X (x_1x_0) and Y (y_1y_0) using one 4x16 decoder. (3 marks)



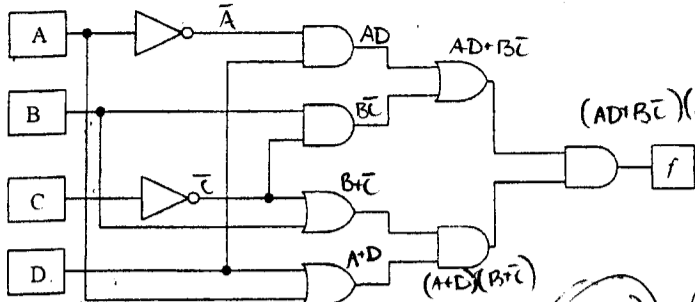
Q3. Design a 4x2 priority encoder (D_3-D_0 ; D_0 is the LSB and has the highest priority; D_3 has the lowest priority). (3 marks)



Q4. Draw the truth table for the following function: $f = \bar{a}b + \bar{a}bc$. Implement the function using two 2x1 MUX. (2+2=4 marks)

a	b	c	f
0	0	0	0

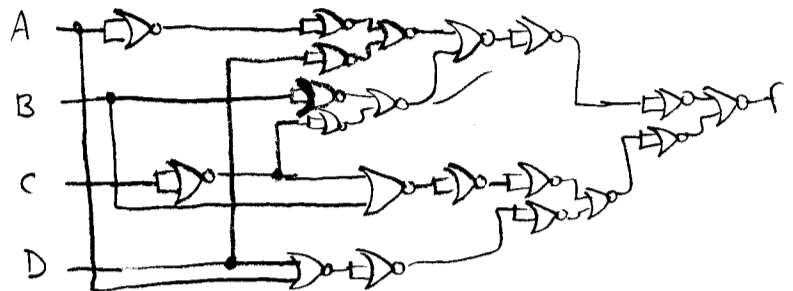
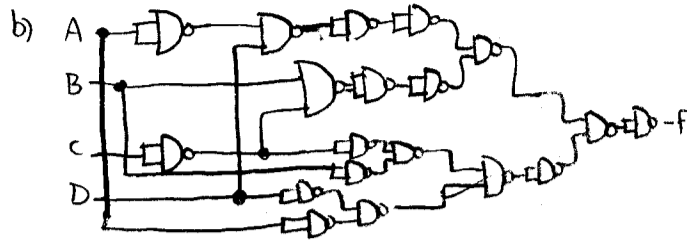
Q5. Consider the following circuit. (a) Determine the circuit's function, $f(A, B, C, D)$; (b) Implement the circuit using only 2-input NAND gates; (c) Implement the circuit using only 2-input NOR gates; (d) Between (a) and (b), which implementation is more efficient (in terms of number of gates)? (1+2+2+1=6 marks)



a) $F = (AD + B\bar{C})(A + D)(B + \bar{C})$

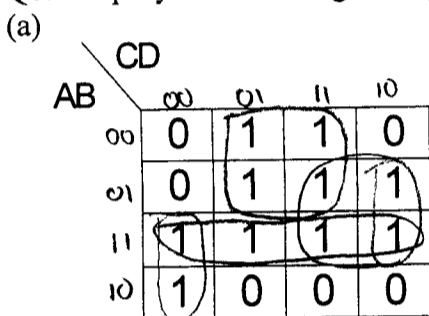
d) NAND implementation is more efficient.

(5)

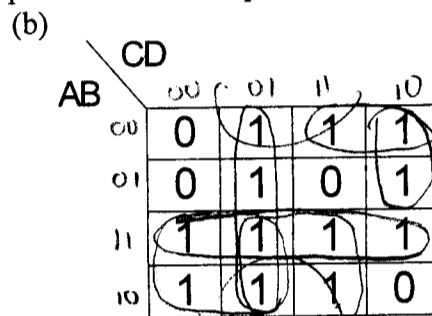


Q6. Simplify the following K-maps and write down the simplified Boolean expressions.

(1+1=2 marks)

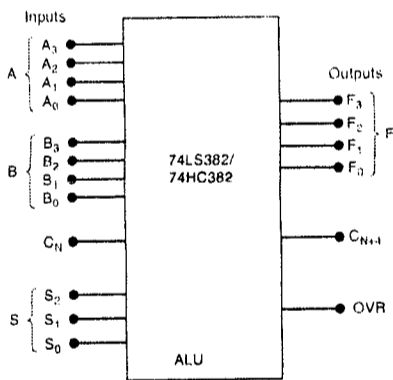


$AB + A\bar{C}\bar{D} + \bar{A}D + BC$
 $= A(B + \bar{C}\bar{D}) + \bar{A}D + BC$



$A\bar{C} + \bar{C}D + \bar{A}D + AB + \bar{A}\bar{C}\bar{D} + \bar{A}\bar{B}C$
 $= A(\bar{C} + D + B) + \bar{C}D + \bar{A}(\bar{C}\bar{D} + \bar{B}C)$

Q7. Consider the following 74LS382 IC. Using minimum number of this IC, design a circuit that produces a HIGH output (1-bit) only when $A(A_3A_2A_1A_0) = B(B_3B_2B_1B_0)$. No external gates can be used. (3 marks)



A = 4-bit input number
 B = 4-bit input number
 C_N = carry into LSB position
 S = 3-bit operation select inputs

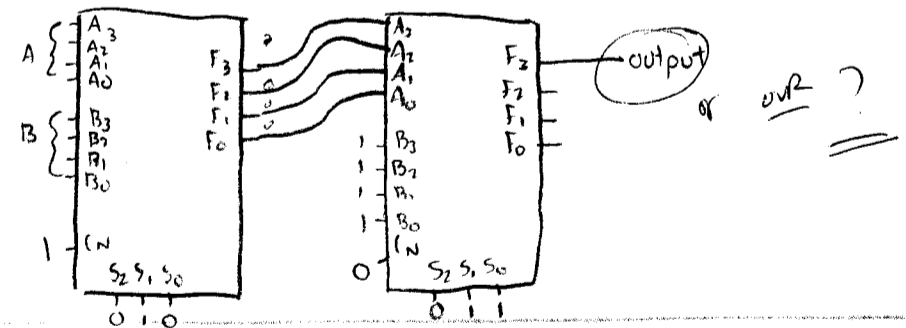
F = 4-bit output number
 C_{N+1} = carry out of MSB position
 OVR = overflow indicator

(a)

S_2	S_1	S_0	Operation	Comments
0	0	0	CLEAR	$F_3F_2F_1F_0 = 0000$
0	0	1	B minus A	Needs $C_N = 1$
0	1	0	A minus B	
0	1	1	A plus B	Needs $C_N = 0$
1	0	0	A \oplus B	Exclusive-OR
1	0	1	A + B	OR
1	1	0	AB	AND
1	1	1	PRESET	$F_3F_2F_1F_0 = 1111$

Notes: S inputs select operation.
 OVR = 1 for signed-number overflow.

(b)



method: A-B
 if = 0, result is high

$$\begin{array}{r} 0100 \\ 1111 \\ \hline 1001 \end{array} \begin{array}{r} 0001 \\ 1111 \\ \hline 0000 \end{array}$$
 ← MSB is output
 if non-zero binary number is added to 1111, MSB=0