

University of Saskatchewan  
Department of Electrical Engineering  
EE 868.3 Digital Techniques for Power System Measurements (Term 1)  
Final Examination (Classroom Examination)

Examination Paper Hand-In Time: 9:00 am, Dec.19, '07  
Instructor: Dr. Rama Gokaraju

Return Time: 5:00pm  
Total Marks: 50

**Instructions:**

- 1) **Important:** After the exam, return the question paper along with your answer booklets (including the unused ones).
- 2) This examination paper consists of 6 problems and 3 pages in total.
- 3) However, you are not permitted to discuss or take assistance of others to solve the examination problems. You would be severely penalized if your solutions point to the above.
- 4) Your solutions should be methodical. You would be penalized if your solutions are illegible.
- 5) Mark allotted for each problem is shown on the right margin.

**Problem 1**

Perform the arithmetic operations  $(+52) + (-17)$  and  $(-52) - (-17)$  in binary using signed-2's complement representation for negative numbers.

A fixed-point binary number system has 1 whole bit and 15 fractional bits. Represent decimal fraction 0.3 in the unsigned format. Represent decimal fraction -0.3 in the 2's-complement format.

0.010011001100110  
1.101100110011010

Show the representation of the decimal number -6.25 in the ANSI/IEEE short and long floating-point format. If the number is not exactly representable, use the round operation.

1 10000001 1001000...

**7.5 Marks**

**Problem 2**

What is the transfer function for the RLC filter in Figure 1. Determine its poles and zeros.

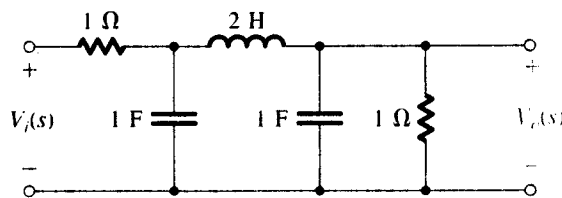


Figure 1

**7.5 Marks**

**Problem 3**

Draw the block diagram of a Dual-Ramp Converter and explain briefly its principle of operation.

**5 Marks**

**Problem 4**

Design a 8-bit successive approximation converter to convert 55.4 Volts into its digital value.

00110111

**5 Marks**

**Problem 5**

Suppose a current signal consists of two sine and cosine components and a noise component as follows:

$$z(t) = x_1 \cos \omega_0 t - x_2 \sin \omega_0 t + d(t)$$

where  $x_1$  and  $x_2$  are the independent variables and  $d(t)$  is the measurement noise. The fundamental frequency is 60 Hz. The signal is sampled at 720 Hz.

The quantized values of its samples are listed below:

| Sample No | Quantized Value | Sample No | Quantized Value | Sample No | Quantized Value |
|-----------|-----------------|-----------|-----------------|-----------|-----------------|
| 1         | 698             | 9         | -270            | 17        | -437            |
| 2         | 554             | 10        | 95              | 18        | -656            |
| 3         | 264             | 11        | 435             | 19        | -699            |
| 4         | -100            | 12        | 656             | 20        | -553            |
| 5         | -431            | 13        | 700             | 21        | -261            |
| 6         | -657            | 14        | 559             | 22        | 94              |
| 7         | -693            | 15        | 261             | 23        | 439             |
| 8         | -551            | 16        | -102            | 24        | 659             |

Use the Discrete Fourier Transform Technique to estimate the magnitudes of  $x_1$  and  $x_2$ . Show the steps of the technique clearly. Show the numerical steps clearly for one sample number.

**10 Marks**

$$x_1 = 700 \quad x_2 = 100$$

**Problem 6**

Suppose a current signal consists of two sine and cosine components, a decaying dc component and a noise component as follows:

$$z(t) = x_1 \cos \omega_0 t - x_2 \sin \omega_0 t + x_3 e^{-t/\tau} + d(t)$$

where  $x_1$ ,  $x_2$  and  $x_3$  are the independent variables and  $d(t)$  is the measurement noise. The fundamental frequency is 60 Hz. The signal is sampled at 720 Hz.

The quantized values of its samples are listed below:

| Sample No | Quantized Value | Sample No | Quantized Value | Sample No | Quantized Value |
|-----------|-----------------|-----------|-----------------|-----------|-----------------|
| 1         | 779             | 13        | 698             | 25        | 697             |
| 2         | 555             | 14        | 556             | 26        | 553             |
| 3         | 263             | 15        | 257             | 27        | 269             |
| 4         | -101            | 16        | -97             | 28        | -94             |
| 5         | -440            | 17        | -440            | 29        | -431            |
| 6         | -652            | 18        | -658            | 30        | -660            |
| 7         | -699            | 19        | -696            | 31        | -701            |
| 8         | -552            | 20        | -559            | 32        | -557            |
| 9         | -265            | 21        | -265            | 33        | -262            |
| 10        | 96              | 22        | 98              | 34        | 98              |
| 11        | 439             | 23        | 442             | 35        | 434             |
| 12        | 656             | 24        | 656             | 36        | 655             |

Design a least squares filter for estimating  $x_1$ ,  $x_2$  and  $x_3$ . Also estimate the time period of the decaying dc component. Use a 7 sample data window.

Show how the [A] matrix will look like. Show the numerical steps clearly for one sample number.

**15 Marks**



$$\begin{aligned}
 & x_1 \cos(\omega t + \theta_1) - x_2 \sin(\omega t + \theta_2) + x_3 e^{-t/\tau} \\
 & x_1 (\cos \omega t \cos \theta_1 - \sin \omega t \sin \theta_1) - x_2 (\sin \omega t \cos \theta_2 + \cos \omega t \sin \theta_2) \\
 & x_1 \cos \theta_1 \cos \omega t - x_1 \sin \theta_1 \sin \omega t - x_2 \sin \theta_2 \cos \omega t - x_2 \cos \theta_2 \sin \omega t + x_3 - x_3 \frac{t}{\tau} \\
 & y_3 = 0
 \end{aligned}$$